

## **Influence of the moisture-tension parameter on sedigraphs and hydrographs from a semiarid region in Brazil**

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**Abstract** Several sorts of models of various complexities have been used for predicting erosion but before simulating the sediment yield, the infiltration process must be simulated. In the infiltration process the main parameters consist of the soil moisture content and suction; thus these parameters can be combined in one single moisture-tension parameter as represented by  $N_s$  in the Green & Ampt infiltration equation. This paper discusses the effect of this parameter on hydrographs and, subsequently, sedigraphs, using data from a test field located in a typical semiarid area in Brazil simulated with a runoff-erosion kinematic model.

### **INTRODUCTION**

Predicting sediment yield using kinematic cascade models has become a useful tool since Brakensiek (1967) introduced this concept. The theory of kinematic flow was first set forth by Lighthill & Whitham (1955) when they published a paper dealing with flood movement in rivers, but the kinematic wave technique was first applied to flow over a sloping plane by Henderson & Wooding (1964). However, in order to model the runoff-erosion process special care must be taken when the infiltration for a given event is estimated. The increase of semiarid areas in the world has brought the aim of much research to the delicate problem of runoff-erosion by heavy rainfall in the area. Physically-based distribution models have been used to predict the runoff-erosion process for such areas, and herein a model of this sort is presented and tested. However, attention has mainly been given to modelling the infiltration process, including the estimation of parameters involved in this particular process such as the moisture-tension parameter in the Green & Ampt infiltration equation, because it affects the sediment yield directly since it controls rainfall excess. This parameter depends mainly on the antecedent condition of the soil, which is difficult to estimate without a permanent measuring system on site. Thus, a better way to estimate such a parameter would be a relationship between two single variables, because this would simplify the whole process of estimating this parameter according to all conditions that have an influence, such as rainfall intensity, duration, and so forth. A simple relationship between the moisture-tension parameter and the number

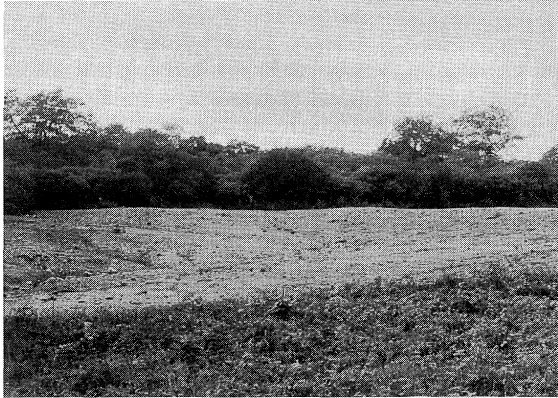


Fig. 1 View of the selected micro-basin with a bare surface.

of antecedent dry days to a rainfall event is proposed.

Particular attention will be given to runoff hydrographs and sedigraphs for different initial infiltration capacities and various types of rainfall, using data obtained from an experimental basin in a semiarid area of Brazil, through which the complex infiltration process during a rainfall event and the behaviour of the moisture-tension parameter according to the number of antecedent dry days are discussed.

## DATA

The selected micro-basin is located in the experimental basin of Sumé, which has been operated since 1972 (Cardier & Freitas, 1982) by UFPB (Federal University of Paraíba, Brazil), SUDENE (Superintendency of Northeast Development, Brazil) and ORSTOM (French Office of Scientific Research and Technology for Overseas Development). This was used to obtain data concerning runoff and sediment yield produced by heavy rainfall in a natural environment. The experimental basin incorporates four micro-basins, nine experimental plots, one sub-basin, and several micro-plots operated by simulated rainfall. Each micro-basin or experimental plot has different surface conditions and slope.

The selected micro-basin (Fig. 1) has an area of 5200 m<sup>2</sup>, mean slope of 7.1% and a perimeter of 302 m. Its soil is classified as brown non calcic "vertic" soil, which is typical of most Brazilian semiarid regions. Several rainfall events were chosen between 1987 and 1988 based on the work of Santos *et al.* (1994). This period was selected because during this time there was no vegetation cover.

## RUNOFF-EROSION MODEL

Lopes (1987) developed a physically-based, distributed parameter, event-oriented, nonlinear, numerical model named the Watershed Erosion Simulation Program (WESP), which computes runoff and sediment yield based on the kinematic waves

assumption. It was especially developed for small basins, which was the reason why this model was chosen in this paper.

The infiltration process is modelled using the Green & Ampt equation and Darcy's law during a steady rain, which can be written in the form, after the beginning of overland flow:

$$f(t) = K_s \left( 1 + \frac{N_s}{F(t)} \right) \tag{1}$$

where  $f(t)$  is the infiltration rate ( $\text{m s}^{-1}$ ),  $K_s$  is the effective soil hydraulic conductivity ( $\text{m s}^{-1}$ ),  $F(t)$  is the cumulative depth of infiltrated water (m),  $t$  is the time variable (s), and  $N_s$  is the soil moisture-tension parameter (m), which can be represented as:

$$N_s = (1 - S_e) p S \tag{2}$$

where  $p$  is the effective porosity ( $0 < p < 1$ ),  $S$  is the average suction at the wetting front (m) and  $S_e$  is relative effective saturation equal to  $\theta_i/\theta_s$ , with  $\theta_i$  as the initial soil moisture content and  $\theta_s$  as the soil moisture content at saturation.

The overland flow caused by rainfall excess is considered one dimensional. Manning's turbulent flow equation is given by:

$$u = \frac{1}{\pi} R_H^{2/3} S_f^{1/2} \tag{3}$$

where  $R_H(x, t)$  is the hydraulic radius (m),  $u$  is the local mean flow velocity ( $\text{m s}^{-1}$ ),  $S_f$  is the friction slope, and  $n$  is the Manning friction factor of flow resistance. Here the assumption of the kinematic approximation that the friction slope is equal to the plane slope ( $S_0 = S_f$ ) is used; i.e. the gravity and friction components are the dominant factors of the momentum equation. This approximation results in the local velocity equation for planes ( $R_H = h$ ):

$$u = \alpha h^{m-1} \tag{4}$$

where  $h$  is the depth of flow (m),  $\alpha$  (equal to  $(1/n)S_0^{1/2}$ ) and  $m$  (equal to  $5/3$ ) are parameters related to surface roughness and geometry, respectively.

Sediment transport is considered as the erosion rate in the plane reduced by the deposition rate within the reach. The erosion occurs due to raindrop impact as well as surface shear. The sediment continuity equation is used to express the sediment transport rate in the reach as a function of the concentration, the discharge and the depth. The equation is solved numerically with a four-point implicit finite-difference scheme to calculate the sediment flow as a function of time and distance. The sediment flux  $\Phi$  ( $\text{kg m}^{-2} \text{s}^{-1}$ ) to the flow is written as:

$$\Phi = e_l + e_r - d \tag{5}$$

where  $e_l$  is the rate of sediment detachment by rainfall impact,  $e_r$  is the rate of sediment detachment by shear stress, and  $d$  is the rate of sediment deposition. The rate  $e_l$  ( $\text{kg m}^{-2} \text{s}^{-1}$ ) is obtained from the relationship:

$$e_l = K_f I r_e \tag{6}$$

in which  $K_f$  is the soil detachability parameter ( $\text{kg s m}^{-4}$ ),  $I$  is the rainfall intensity

( $\text{m s}^{-1}$ ), and  $r_e$  is the effective rainfall ( $\text{m s}^{-1}$ ). The rate  $e_R$  ( $\text{kg m}^{-2} \text{s}^{-1}$ ) is expressed by the relationship:

$$e_R = K_R \tau^{1.5} \quad (7)$$

where  $K_R$  is a soil detachability factor for shear stress ( $\text{kg m N}^{-1.5} \text{s}^{-1}$ ), and  $\tau$  is the effective shear stress ( $\text{N m}^{-2}$ ), which is given by:

$$\tau = \gamma R_H S_f \quad (8)$$

where  $\gamma$  is the specific weight of water ( $\text{N m}^{-3}$ ); and  $d$  ( $\text{kg m}^{-2} \text{s}^{-1}$ ) is expressed as:

$$d = \varepsilon V_s C \quad (9)$$

where  $\varepsilon$  is a coefficient that depends on the soil and fluid properties (set to 0.5 in this study),  $V_s$  is the particle fall velocity ( $\text{m s}^{-1}$ ), and  $C(x, t)$  is the sediment concentration in transport ( $\text{kg m}^{-3}$ ).

The concentrated flow in the channels is also described by continuity and momentum equations. The momentum equation can be reduced to the discharge equation with the kinematic wave approximation:

$$Q = \alpha A R_H^{m-1} \quad (10)$$

where  $A$  is the area of flow ( $\text{m}^2$ ). The net sediment flux  $\Phi_c$  ( $\text{kg m}^{-1} \text{s}^{-1}$ ) for the channel is expressed by:

$$\Phi_c = q_s + e_r - d_c \quad (11)$$

where  $q_s$  is the lateral sediment inflow into the channel ( $\text{kg m}^{-1} \text{s}^{-1}$ ),  $e_r$  is the erosion rate of the bed material ( $\text{kg m}^{-1} \text{s}^{-1}$ ) obtained from the relation:

$$e_r = a(\tau - \tau_c)^{1.5} \quad (12)$$

in which  $a$  is the sediment erodibility parameter, and  $\tau_c$  is the critical shear stress for sediment entrainment ( $\text{N m}^{-2}$ ), which is given by the relationship:

$$\tau_c = \delta(\gamma_s - \gamma)d_s \quad (13)$$

where  $\delta$  is a coefficient (0.047 in the present study),  $\gamma_s$  is the specific weight of sediment ( $\text{N m}^{-3}$ ) and  $d_s$  is the mean diameter of sediments (m).

The deposition term  $d_c$  ( $\text{kg m}^{-1} \text{s}^{-1}$ ) in equation (11) is expressed by

$$d_c = \varepsilon_c T_w V_s C \quad (14)$$

in which  $\varepsilon_c$  is the deposition parameter for channels, considered as unity in the present case,  $T_w$  is the flow top width (m) and the other terms are as defined in equation (9).

## MODEL PARAMETERS

### The parameters

Most of the parameters shown here can be assumed constant either as universally

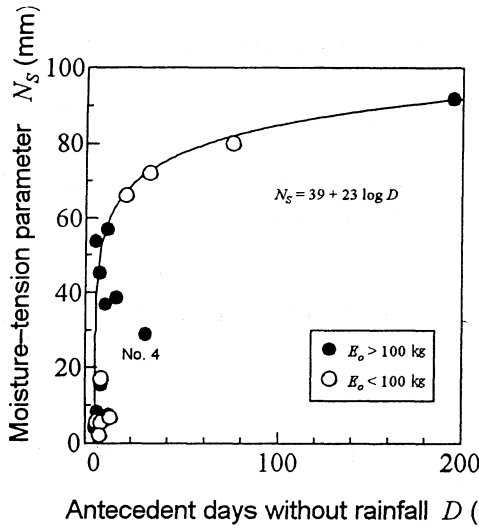


Fig. 2 Relationship between  $N_s$  and the number of antecedent dry days  $D$ .

constant or specific for this studied area. The Manning friction factor of flow resistance can be assumed as 0.02 for planes and 0.03 for channels, the specific weight of water as  $9779 \text{ N m}^{-3}$ , and the specific weight of sediment as  $25\,914\,250 \text{ N m}^{-3}$ .

The remaining parameters are specific for this area. The effective soil hydraulic conductivity  $K_s$  was assumed equal to  $5.0 \text{ m s}^{-1}$  based on tests conducted in the field, and the others were calibrated by optimization using the Standardized Powell method (Powell, 1964), i.e.  $K_R$  equal to  $2.1 \text{ kg m N}^{-1.5} \text{ s}^{-1}$ ,  $K_I$  equal to  $5.1 \times 10^8 \text{ kg s m}^{-4}$ , and  $a$  equals  $0.015 \text{ kg m}^2 \text{ N}^{-1.5} \text{ s}^{-1}$ .

Finally, the moisture-tension parameter could not be assumed constant because the moisture condition changes according to the rainfall event. However, a relationship between  $N_s$  and the number of antecedent dry days (Fig. 2) was found by

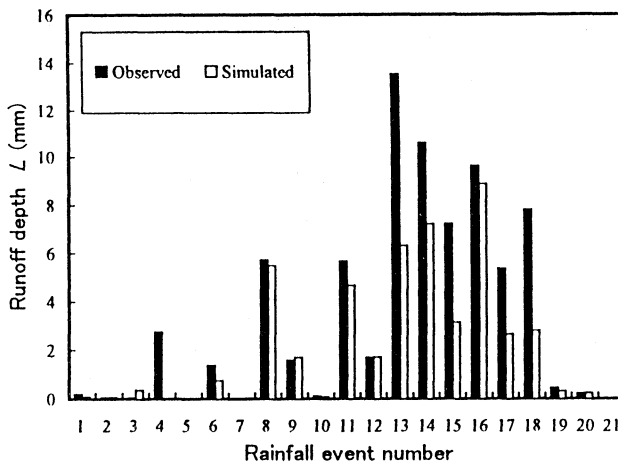


Fig. 3 Observed and simulated total runoff depths.

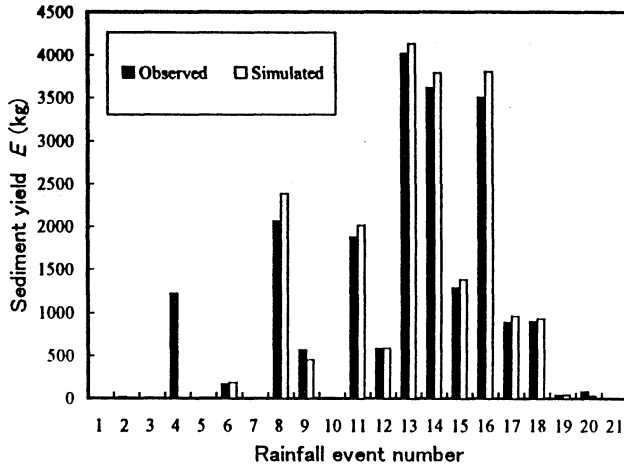


Fig. 4 Observed and simulated total sediment yields.

the authors as presented in Santos *et al.* (1994). This curve is very useful because the  $N_s$  parameter depends on several conditions but using Fig. 2 the parameter can be estimated just by one single condition, which is the number of days without rainfall between two consecutive events. Comparisons between the observed and calculated runoff depth  $L$  and sediment yield  $E$ , using the proposed  $N_s$  curve and the optimized parameters, are shown in Figs 3 and 4, respectively. As the parameter  $N_s$  has a strong influence on the hydrograph shape, it will be discussed separately in the next section.

### Influence of $N_s$ values

Figure 5 is an example of a simulated runoff, which shows how a variation of the  $N_s$  value can change the runoff hydrograph from the test field by the rainfall given in the

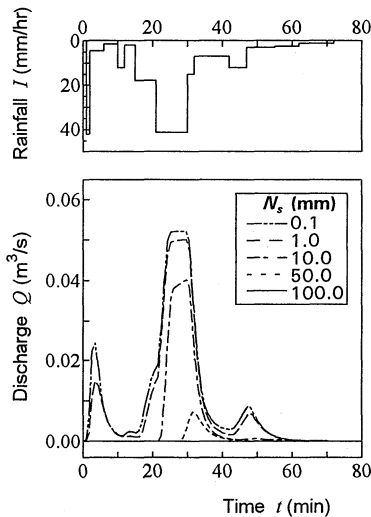


Fig. 5 Hydrograph and hietograph for event no. 11 with different  $N_s$  values.

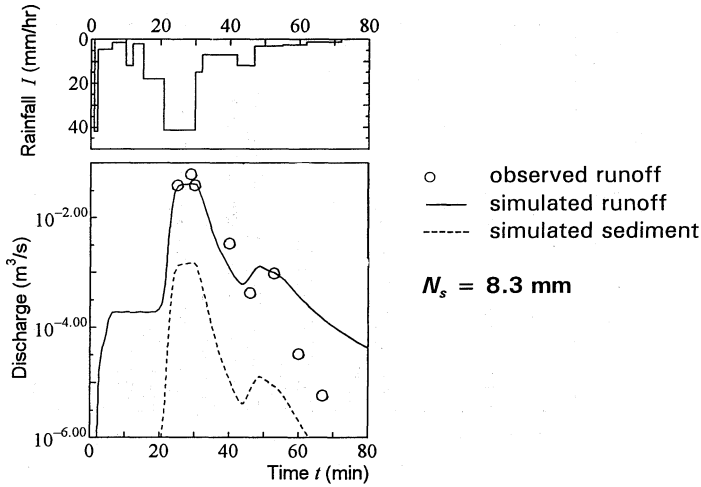


Fig. 6 Hydrograph and hyetograph with sedigraph for event no. 11.

figure. The number of antecedent dry days for this event was less than one day, and the optimized  $N_s$  is 8.3 mm. In the case of  $N_s$  equal to 10 mm, runoff occurs only when  $t > 20$  min. If the  $N_s$  value decreases, a discharge peak will appear at the beginning of the rainfall, which was not observed in the field as shown in Fig. 6. If the  $N_s$  value becomes greater, the runoff will decrease and the last peak in the hydrograph will disappear, since infiltration has become greater. The moisture-tension parameter  $N_s$  can be seen to have a strong influence on the shape of the hydrograph.

Figures 6–10 show the sedigraphs and the comparison between the simulated hydrograph and the observed discharge data for several selected rainfall events, in which the observed discharge data are plotted in dots, and the calculated ones are plotted by a line, where the initial time ( $t = 0$  min) for the measurement of discharge was different from that of rainfall, and the observed time was adjusted for some

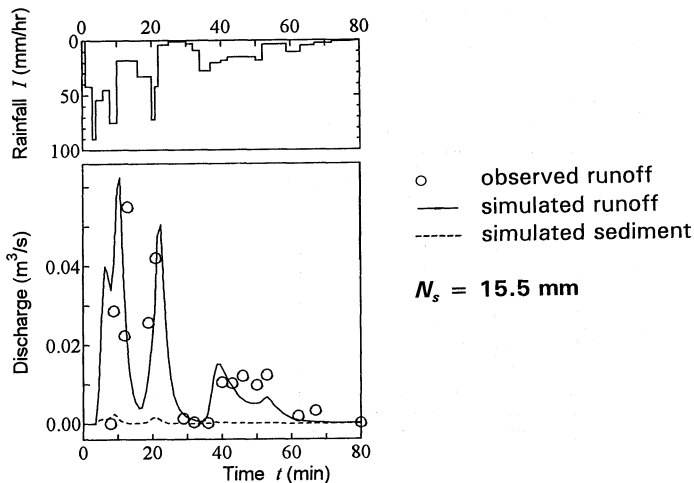


Fig. 7 Hydrograph and hyetograph with sedigraph for event no. 16.

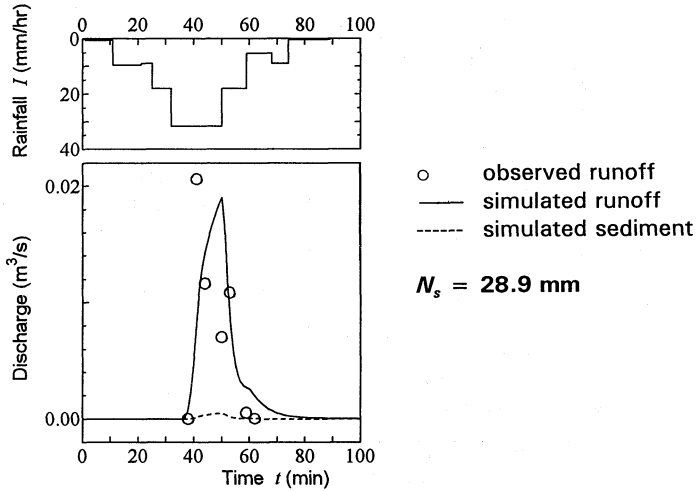


Fig. 8 Hydrograph and hietograph with sedigraph for event no. 4.

events. Unfortunately, the measurement equipment in the micro-basin is conceived to collect just the total sediment yield.

Typical events with several different values of  $N_s$ , which range from 8.3 to 91.8 mm were selected with the first event plotted on a logarithmic scale to allow for an understanding of the relationship between the runoff and sediment discharges. The simulated runoff and sediment yield values seem to approximate the observed ones on the whole as shown in Figs 3 and 4. However, the degree of agreement seems to be different according to the values of  $N_s$ . For smaller values of  $N_s$ , which are for the rainfall events that occur a short time after the previous rainfall, the simulated hydrographs seem to follow the observed data very well for the simple hydrograph as shown in Fig. 6 as well as for complex rainfall patterns as shown in Fig. 7. On the other hand, the simulated hydrographs for large values of  $N_s$  do not follow the variation of the observed discharge data very well as shown in Figs 9 and 10. More

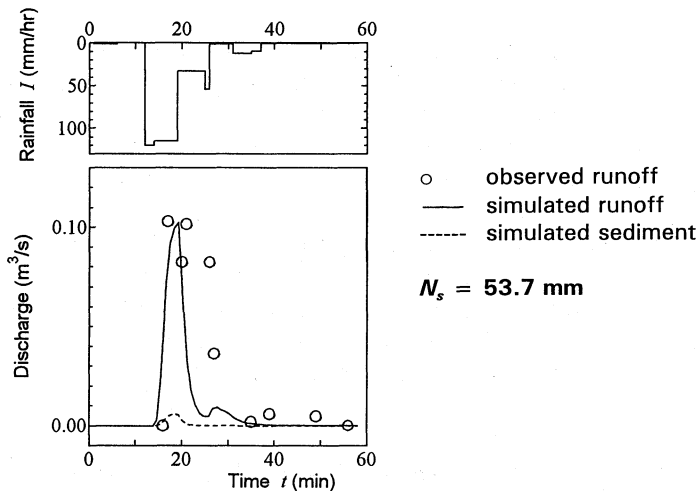


Fig. 9 Hydrograph and hietograph with sedigraph for event no. 13.



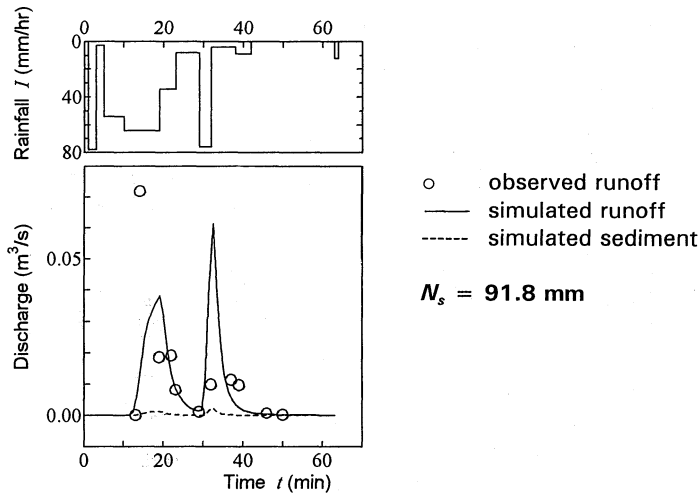


Fig. 10 Hydrograph and hyetograph with sedigraph for event no. 8.

accurate consideration of the  $N_s$  values for dry conditions of soil is needed. In addition, as shown in Fig. 2, the  $N_s$  value can range from near zero up to 60 mm when the number of dry days  $D$  is very small.

## CONCLUSIONS

The runoff-erosion process, using data obtained from an experimental basin in a semiarid region of Brazil, was studied. The obtained conclusions are summarized below.

- The moisture-tension parameter  $N_s$  in the test basin is proved to depend mainly on the number of days  $D$  between the consecutive storms, and the relationship between  $N_s$  and  $D$  is determined for the basin, for example  $N_s = 90 \text{ mm}$  for  $D > 50$  days, and  $N_s$  varies from 0 to 60 mm within a few antecedent days without rainfall.
- Generally, the simulated sediment yields and runoff depths seem to approximate the observed ones. However, the degree of agreement seems to be different according to the values of  $N_s$ . For smaller values of  $N_s$ , which are for the rainfall events occurring a short interval after the previous rainfall event, the simulated hydrographs appear to follow the observed data very well for both the simple hydrograph, and for complex rainfall patterns.
- On the other hand, the simulated hydrographs for large values of  $N_s$  do not follow the variation of the observed discharge data very well. More accurate consideration of the  $N_s$  values for dry conditions of soil is needed. In addition, the determination of  $N_s$  for wet conditions is difficult because it can range from near zero up to 60 mm according to the proposed curve.

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