# Surface resistance calibration for a hydrological model using evapotranspiration retrieved from remote sensing data in Nahe catchment forest area

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**Abstract** In this paper, a method combining graphical and statistical techniques is proposed for surface resistance calibration in a distributed hydrological model, WaSiM-ETH, by comparing daily evapotranspiration simulated by model WaSiM-ETH with corresponding daily evapotranspiration retrieved from remote sensing images. The study area locates in Nahe catchment (Rhineland-Palatinate, Germany,  $4065 \text{ km}^2$ ) forest regions. The remote sensing based observations are available for a very limited number of days but representative for most soil moisture conditions. By setting canopy resistance ( $r_s$ ) at 150 s/m, soil surface resistance ( $r_s$ ) at 250 s/m or at 300 s/m for deciduous forest and setting  $r_c$  at 300 s/m,  $r_{sc}$  at 600 s/m or at 650 s/m for pine forest, the model exhibits its best overall performance in space and time. It is also found that with sufficient soil moisture, the model exhibits its best performance in space scale.

**Key words** surface resistance calibration; distributed hydrological model WaSiM-ETH; evapotranspiration; remote sensing images; soil water conditions

#### INTRODUCTION

The Penman-Monteith (PM) equation is widely used for evapotranspiration estimation. In the equation, surface resistance (r<sub>s</sub>) is a critical parameter, to which the evapotranspiration is highly sensitive, especially in dry canopy (no-rainfall) cases in forest (Beven, 1979). It is described as the bulk resistance of all transmission mediums such as crop, soil and others (Li *et al.*, 2013). Surface resistance is difficult to specify and usually obtained from the literature or by empirical means (Farahani *et al.*, 2007). In 1998, the Food and Agriculture Organization of the United Nations (FAO) gave a fixed surface resistance at 70 s/m for a crop with a uniform height of 0.12 m (Allen *et al.*, 1998). A further recommendation is to use a surface resistance of 50 s/m for daytime and 200 s/m for night-time (Allen *et al.*, 2006). It is also recognized that surface resistance always varies between 50 s/m and 200 s/m for grass and 100 s/m and 400 s/m for forest (Rana *et al.*, 1998). For no-rainfall conditions in forest regions, the canopy resistance (r<sub>c</sub>) and soil surface resistance (r<sub>se</sub>) are further defined, since actual evapotranspiration mainly comes from transpiration from plant leaves and evaporation of bare soil between plants. Interception evaporation is not taken into account due to its negligible contribution with a dry canopy.

Model performance evaluation by comparing model-simulated outputs with corresponding observations is fundamental to hydrological model calibration. For decades, remote sensing images were frequently used for hydrological state variables or heat fluxes in water cycle retrieval, especially in basins with sparse or few data available. These remote sensing based outputs are quite a popular alternative to traditional observations gauged from climate stations. They are superior to traditional observations and model simulations in the space scale, since the latter are both interpolated grid outputs whose spatial patterns depend on the locations and numbers of climate stations. However, multiple factors such as the scan cycle of satellites, the running status of the equipment and the weather conditions at the data acquisition time lead to only a limited number of high quality remote sensing images in specific time periods being available. Nouri *et al.* (2014) summarized that the uncertainty in aerodynamic components estimation and errors in narrow vegetation areas, such as riparian zones measurement, are also noted shortages of use of remote sensing techniques to measure evapotranspiration.

This study proposes a method for surface resistance calibration of the WaSiM-ETH model based on a limited number of observations in time series retrieved from remote sensing images.

#### MATERIAL AND METHODS

### Study area

The study area is Nahe catchment locating in the state of Rhineland-Palatinate, southwest Germany (Fig. 1). The River Nahe is about 120 km in length, rising from the Saarland and joining the River Rhine at Bingen. The drainage basin is in total 4065 km<sup>2</sup>. This area is famous for grape cultivation and quality wine production due to its moderate climate. The average elevation of the entire Nahe catchment is 353 m while in the north and west regions it ranges from 300 m to 817 m. This area is highly wooded; deciduous forest and pine forest are the two primary forest types.

Nahe catchment has long been known as a flood prone area. Residents settle along the River Nahe and its tributaries have suffered a lot from flood damages. The recent huge flood events in this region occurred in 1993 and 1995.

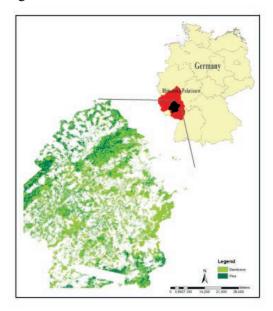


Fig. 1 Location and forest distribution of Nahe catchment

# Hydrological model

WaSiM-ETH (Water Flow and Balance Simulation Model, first developed at the ETH Zurich in Switzerland) is a distributed, deterministic, mainly physical and grid-based hydrological model (Schulla and Jasper, 2007). In this study, a long-term simulation from 1971 to 2003, with a daily time step, was conducted. Meteorological data such as sunshine duration, air temperature, relative humidity, wind speed and precipitation selected from 15 climate stations were employed. The potential evapotranspiration (ETP) was first estimated by the Penman-Monteith approach (Monteith, 1975, Brutsaert, 1982). The formulation is:

$$\lambda E = \frac{3.6 \cdot \frac{\Delta}{\gamma_p} (R_n - G) + \frac{\rho \cdot C_p}{\gamma_p \cdot r_a} (e_S - e) \cdot t_i}{\frac{\Delta}{\gamma_p} + 1 + r_S / r_a} \tag{1}$$

where  $\lambda$  is the latent vaporization, E is the latent heat flux,  $\Delta$  is the tangent to the saturated vapour pressure curve,  $R_n$  is the net radiation, G is the soil heat flux,  $\rho$  is the density of dry air,  $C_p$  is the specific heat capacity of dry air at constant pressure,  $e_s$  is the saturation vapor pressure at temperature T, e is the actual vapour pressure,  $t_i$  is the number of seconds within a time step,  $\gamma_p$  is the psychrometric constant,  $r_s$  is the bulk-surface resistance and  $r_a$  is the bulk-aerodynamic resistance.

In the model, transpiration from plants and evaporation from bare soil were separately calculated by equation (1). Canopy resistance ( $r_{sc}$ ) and soil surface resistance ( $r_{sc}$ ) are the separate corresponding surface resistances. According to the actual soil moisture, actual evapotranspiration (ETA) was then obtained based on ETP. All soil water conditions are considered:

$$ETA_{i} = 0 \qquad \qquad \Theta(\psi) < \Theta_{wp}$$

$$ETA_{i} = ETP_{i} \cdot (\Theta(\psi_{i}) - \Theta_{wp}) / (\Theta_{\psi g} - \Theta_{wp}) \qquad \qquad \Theta_{wp} \leq \Theta(\psi) \leq \Theta_{\psi g} \qquad (2)$$

$$ETA_{i} = ETP_{i} \qquad \qquad \Theta(\psi) \leq \eta \cdot \Theta_{sat}$$

$$ETA_{i} = ETP_{i} \cdot (\Theta_{sat} - \Theta(\psi_{i})) / (\Theta_{sat} - \eta \cdot \Theta_{sat}) \qquad \qquad \eta \cdot \Theta_{sat} < \Theta(\psi) \leq \Theta_{sat}$$

where i is the index of the soil layer,  $\Theta$  ( $\psi$ ) is the actual relative soil water content at suction  $\psi$ ,  $\eta$  is the maximum relative soil water content without partly or totally anaerobic conditions,  $\Theta_{\text{sat}}$  is the saturation water content of the soil,  $\Theta_{\psi_g}$  is the soil water content at a given suction  $\psi_g$ ,  $\Theta_{\text{wp}}$  is the soil water content at the permanent wilting point.

#### Remote sensing

A modification of simplified method is used for daily evapotranspiration estimation by remote sensing images. The simplified method was firstly proposed by Jackson *et al.* (1977), in which the sensible heat flux is linearly related to the instantaneous temperature difference between surface and air at midday with a constant B, as well as the integrated daily soil heat flux is considered as negligible. Based on the surface energy equation, evapotranspiration is obtained as its energy consumption – the latent heat flux, by subtracting sensible heat flux from net radiation. This method has been improved by a number of studies (Sequin and Itier, 1983; Nieuenhuis *et al.*, 1985; Carlson *et al.*, 1995). An additional exponential coefficient n and a non-constant B are finally employed to retrieve sensible heat flux from surface-air temperature difference. Moreover, both n and B are given as functions of fractional vegetation cover. Casper and Vohland (2008) further considered the contribution of soil heat flux and modified the method as:

$$\int_0^{24h} LE = \int_0^{24h} R_n - G - B(T_{s(max)} - T_{a(max)})^n$$
 (3)

where  $\int_0^{24h}$  LE is the daily latent heat flux for 24 hours,  $R_n$  is the daily net radiation for 24 hours, G is the soil heat flux,  $T_{s(max)}$  is the daily maximal land surface temperature,  $T_{a(max)}$  is the daily maximal near surface air temperature, parameter  $B = 0.0109 + 0.051f_{cov}$ , parameter  $n = 1.067 - 0.372f_{cov}$ , with  $f_{cov}$  is the fractional vegetation cover.

High quality Thematic Mapper (TM) images and Enhanced Thematic Mapper plus (ETM+) images from five separate dates (15 May 2000, 5 July 2001, 19 July, 4 August and 21 September in 2003) were selected from the time period that model run (1971–2003). The summer of 2003 is known as extremely warm and dry in Germany. Bands 1–5 and 7 of both TM and ETM+ images with a spatial resolution of 30 m were used for a series of surface properties achieving: surface albedo, normalized difference vegetation index (NDVI), fractional vegetation cover (F<sub>cov</sub>) and surface emissivity coefficient. Thermal band 6 with a resolution of 120 m for TM and 60 m for ETM+ were applied for land surface temperature (LST) retrieving.

In the following we use "ET" to denote the evapotranspiration simulated from WaSiM-ETH model and "LE" to denote the corresponding evapotranspiration retrieved by remote sensing images. All text, figures and tables will follow this rule.

#### Model performance evaluation

Mean absolute error (MAE) and root mean square error (RMSE) are two similar and widely used measures in model performance evaluation, smaller values of which indicate less mean gross error between two variables. MAE is less sensitive to extreme values compared to RMSE (Fox, 1981) and avoids the physically artificial exponentiation that RMSE has (Willmott, 1982). Willmott and Matsuura (2005) concluded that RMSE is an inappropriate and misinterpreted measure of average

model performance error while MAE is more natural and unambiguous. In this paper, MAE were employed and calculated as:

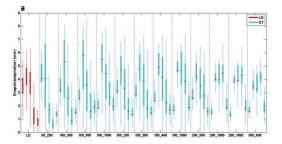
$$MAE = \frac{1}{n} \sum_{i=1}^{n} |e_i| \tag{4}$$

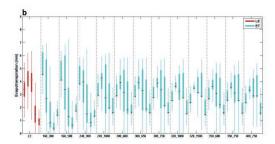
where  $e_i$  (i = 1,2,3 ... n) indicates pixel-wise difference between ET and LE.

# RESULTS AND DISCUSSION

# Temporary pattern

For both forest types, LE at five dates shows similar patterns in time scale (Fig. 2): (1) on 5 July 2001, the median of LE is the top of all, (2) median LE on 19 July 2003 is higher than that on 15 May 2000 and decreases sharply to 4 August 2003, (3) on 21 September 2003 the median LE is the lowest. It is noted that the very low actual evapotranspiration on 4 August 2003 shows a high contrast to those amounts on 5 July 2001 and 19 July 2003, which are also in summer time. For deciduous forest, two ET groups with surface resistance combinations of  $r_{sc}$  at 150 s/m,  $r_{se}$  at 250 s/m, and  $r_{sc}$  at 150 s/m,  $r_{se}$  at 300 s/m (separately denoted as ET group 150\_250 and ET group 150\_300, notation of ET groups with different surface resistance combinations follows the same rule) show similar temporary patterns (Fig. 2(a)). Four groups of ET 300\_600, ET 300\_650, ET 300\_750 and ET 350\_600 for pine forest exhibit similar temporary patterns (Fig. 2(b)) to LE.

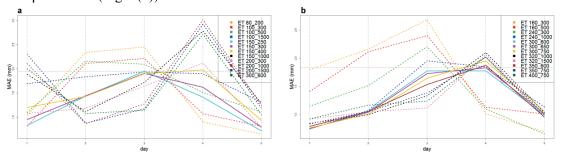




**Fig. 2** Daily evapotranspiration at five dates (in mm, including both LE and ET, with five days each group) in (a) deciduous forest and (b) pine forest. The red boxplots are one LE group as well as the 12 green boxplot groups from ET groups simulated with 12 different surface resistance combinations by WaSiM-ETH. The five sample dates are 15 May 2000, 5 July 2001, and 19 July, 4 August and 21 September 2003, in order.

# Model performance

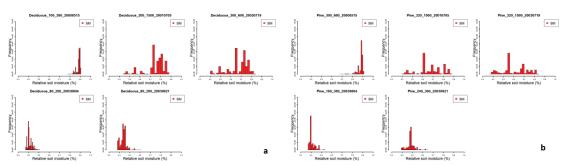
For deciduous forest, five day's MAE between ET 150\_250 and LE and five day's MAE between ET 150\_300 and LE (denoted as MAE group 150\_250 and MAE group 150\_300, denotation of other MAE groups between ET with different surface resistance combinations and LE follow the same rule) indicate relatively better overall model performance (than others) – the MAE of five days are all in relatively small ranges (below the horizontal reference line, Fig. 3(a)). Likewise, groups of MAE 300\_600 and MAE 300\_650 indicate better overall model performance in time scale for pine forest (Fig. 3(b)).



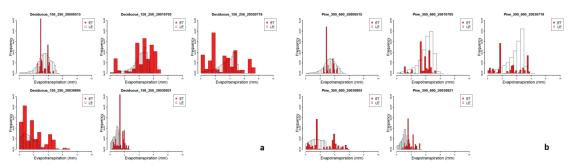
**Fig. 3** Five-days MAE (mean absolute error) between ET (simulated from 12 surface resistance combinations) and LE in (a) deciduous forest and (b) pine forest.

#### Soil water content

In this paper, we assumed that daily soil water content simulated by WaSiM-ETH model with the surface resistance, which the minimal MAE indicates, approaches the reality of that day. With this assumption, the approximate actual soil water content of five separate days in both forest types are roughly inferred (Fig. 4). It is shown that in both forest types, it was wet but unsaturated (the saturated water content point is set as 95% in WaSiM-ETH) on 15 May 2000 when relative soil moisture was mainly distributed in an approximate range from 80% to 91%; 5 July 2001 and 19 July 2003 were medium wet since their soil moisture roughly ranges from 40% to 89%; on 4 August and 21 September 2003 the soil moistures were mainly in the range 35% to 55%, which is really dry.



**Fig. 4** Five days' inferred roughly actual relative soil moisture in root zone in (a) deciduous forest and (b) pine forest.



**Fig. 5** Five days' frequency distribution of (a) ET 150\_250 and LE in deciduous forest and (b) ET 300 600 and LE in pine forest.

As the principal reference while reducing potential evapotranspiration (ETP) to actual evapotranspiration (ETR), actual soil water content determines the magnitude of ET generation. It is also inferred to affect the daily ET performance in the space scale (Fig. 5): ET with sufficient soil water (on 15 May) performs best – including smaller MAE and non-bias error trend, while ET with less soil moisture (on 4 August and 21 September) leads also to lower MAE but obviously to an overestimation. Therefore it is also inferred that ET with a single soil moisture condition (mainly wet or dry unlike that on 5 July and 19 July) exhibits less average gross error. Daily LE and ET show very different spatial distribution (Fig. 5) – the former is continuous while the latter is discontinuous.

#### CONCLUSION

A method combining graphical and statistical techniques for surface resistance calibration in WaSiM-ETH was proposed in this paper. Model performance in both time and space scale have been assessed. Boxplots were used to visually evaluate the temporary similarity between simulations and observations, especially for the extremely event (on 4 August 2003). MAE is employed to measure the daily spatial errors between the paired data sets. Considering multiple soil water conditions, this method covers the shortage of observations retrieved from remote

sensing images, i.e. limited numbers of discontinuous data in a specific time period are available. Soil moisture is inferred to be a critical factor affecting model performance. With sufficient soil moisture, the model simulated ET leads to better performance in the space scale with less average gross error and non-bias error trend. By setting canopy resistance ( $r_{sc}$ ) at 150 s/m and soil surface resistance ( $r_{se}$ ) at 250 s/m or at 300 s/m for deciduous forest, as well as setting  $r_{sc}$  at 300 s/m and  $r_{se}$  at 600 s/m or at 650 s/m for pine forest, comparing ET with LE visually shows similar temporary patterns and statistically exhibits better overall model performance in time and space scale.

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