

Creager and Francou-Rodier envelope curves for extreme floods in the Danube River basin in Croatia

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Abstract This paper presents a comparison of Creager and Francou-Rodier envelope curves for average maximum annual discharges, for the highest observed discharges, and for maximum annual discharges of the 10-, 100- and 1000-year return periods in the Danube River basin in Croatia. They were calculated on the basis of 99 available, sufficiently long and homogenous time series of measured discharges.

Key words Creager's method; Croatia; Danube River basin; envelope curves; Francou-Rodier's method; maximum discharges

INTRODUCTION

The Danube River basin is, after the Volga River basin, the second biggest basin in Europe with a size of about 817 000 km², with 18 riparian states and about 82 million inhabitants.

In Croatia, the Danube River basin (Fig. 1) covers approximately 34 000 km², roughly 60% of the country's land area, where approximately 65% of the total population of the Republic of Croatia live. Major Croatian rivers, such as the Danube, the Sava, the Drava, the Kupa, the Una and the Mura flow through this area. It is located on the Pannonian plain and its rims, with the water divide separating it from the Adriatic catchments running through the Dinaric karst.

The particular socio-economic significance of this area, not only for the Republic of Croatia, but also for a greater region, emphasizes the importance of efficient flood control. Although certain flood control activities in this area date from the 19th century, systematic development of flood control systems did not begin until after the catastrophic floods on the Sava, the Drava and their tributaries during the 1960s. Gradual development of flood control systems in the last four decades has significantly reduced potential damage, a fact proven by the successful reduction of numerous recent floods. Most of the systems constructed are only partially completed, which results in a continuing significant risk of flooding across large areas. Further development of the flood and torrents control systems remains, therefore, one of the strategic tasks of Croatian water management.

Basic information for further planning and design of flood control systems are maximum discharges of required return periods in adequate locations along the water-courses. These can be estimated by applying stochastic methods for sufficiently long and homogenous time series of measured discharges at gauged locations, or by

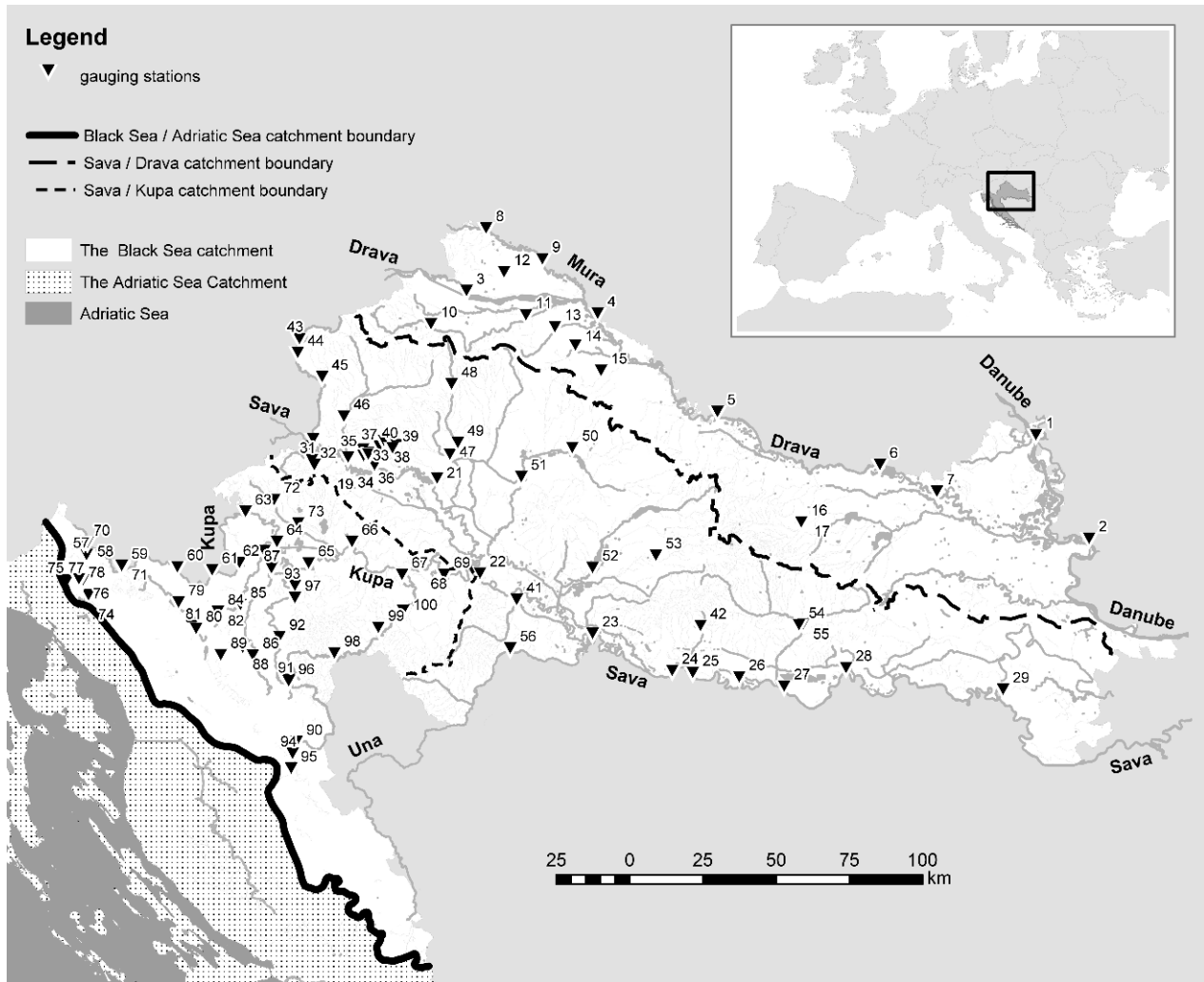


Fig. 1 Overview map of the locations of analysed gauging stations in the Danube River basin in Croatia

deterministic methods at ungauged locations. Common hydrological practice also recognizes the use of various methods for evaluation of reliability of such calculated values. The aim of this paper is to compare two possible methods for evaluation of the reliability of previously estimated values in the Danube catchment area in Croatia: Creager's and Francou-Rodier's envelope curves for average maximum annual discharges, for highest observed discharges, and for maximum annual discharges of the 10, 100 and 1000-year return periods in the Danube River basin in Croatia. Similar investigations for large floods across the whole of Europe were performed by Stanescu & Matreata, 1997.

THEORETICAL APPROACH AND INVESTIGATION PROCEDURE

Creager's envelope curves of specific maximum discharges (Creager & Justin *et al.*, 1945) are formulated as follows:

$$q = aA^{bA^c}$$

where q is specific maximum discharge ($\text{m}^3 \text{s}^{-1} \text{km}^{-2}$); A is catchment area (km^2); and a , b , c are regional parameters.

The Francou-Rodier envelope curves of maximum discharges (Francou & Rodier, 1967) are formulated as follows:

$$\frac{Q}{Q_0} = \frac{A}{A_0}^{1 + \frac{K}{10}}$$

where Q is maximum discharge ($\text{m}^3 \text{s}^{-1}$); A is catchment area (km^2); K is the Francou-Rodier coefficient; $Q_0 = 10^6 \text{ m}^3 \text{s}^{-1}$; and $A_0 = 10^8 \text{ km}^2$.

Creager's and Francou-Rodier's envelope curves for the Danube River basin in Croatia are defined on the basis of available time series of daily discharges which are stored in the hydrological database of the Croatian Meteorological and Hydrological Service (Plantić, 1996).

The theoretical approach described above can be applied only when the series are sufficiently long, homogenous and when there are no significant trends. Analyses of time series homogeneity and trends were performed only for the maximum annual discharge series at all gauging stations on the Danube River basin in Croatia that have observation periods longer than or equal to 25 years (108 stations).

The analyses of homogeneity were performed by application of the Wilcoxon test in such a way that the available series was split into two sub-series, depending on the time of replacement of hydrometric equipment at the stations (rods to limnigraphs) and depending on the timing of construction of major hydrotechnical structures with significant impacts on the water regime (reservoirs, main dykes and distribution structures). The presence of trends in the time series of maximum annual observed discharges was tested using Mann's test. On the basis of the homogeneity and trend analyses performed, 100 time series of maximum annual discharges were selected for further analysis.

The next step was probabilistic analysis of selected time series of maximum annual observed discharges. Maximum annual discharges of 10-year return period were calculated by application of an empirical distribution, and maximum annual discharges of 100 and 1000-year return periods were calculated by applications of the normal distribution (6 stations), log-normal distribution (18 stations), Gamma two-parameter distribution (9 stations), Gumbel distribution (11 stations), Pearson III distribution (27 stations) and log-Pearson III distribution (29 stations). The goodness of fit was tested using the Kolmogoroff-Smirnoff test. The results of the probability analysis of the time series are shown in Table 1.

The last step was to calculate the regional parameters a , b and c of Creager's formula and K of Francou-Rodier's formula for each envelope curve by means of logarithmic and regression analyses. Because of unreliability of the observed and calculated maximum discharges at Petrina gauging station (No. 59) on the Kupa River, these data were excluded from calculations of the regional parameters.

Table 1 Basic characteristics of analysed gauging stations in the Danube catchment area in Croatia.

No.	River	Gauging station	Catchment area (km ²)	Observing period (no. of years)	Discharges Q (m ³ s ⁻¹)			Maximum for return periods (years)		
					Mean	Average max annual	Max obs'd (year of occurrence)	10	100	1000
DANUBE RIVER										
1	Danube	Batina	210250	1951–1989 (39)	2313	4841	8360 (1965)	6322	7860	9288
2	Danube	Erdut	251593	1950–1989 (40)	2852	5443	9250 (1965)	7278	9580	11952
DRAVA RIVER BASIN										
3	Drava	Varaždin	15616	1951–1981 (31)	341	1286	2843 (1966)	1811	2776	3620
4	Drava	Botovo	31038	1961–1998 (38)	514	1596	2652 (1972)	2369	3083	3936
5	Drava	Terezino Polje	33916	1961–1998 (38)	526	1506	2889 (1972)	2382	3190	4420
6	Drava	Donji Miholjac	37142	1926–1998 (71)	543	1360	2288 (1972)	1779	2269	2707
7	Drava	Belišće	38500	1962–1993 (31)	556	1405	2232 (1972)	2021	2573	3242
8	Mura	Mursko Središće	10891	1926–1998 (67)	171	732	1454 (1938)	1180	1651	2179
9	Mura	Goričan	13148	1926–1998 (70)	161	642	1447 (1972)	996	1372	1713
10	Bednja	Željeznica	308	1959–1998 (40)	4.04	59.9	112 (1959)	95.7	153	214
11	Bednja	Ludbreg	547	1947–1998 (52)	7.29	80	179 (1972)	128	172	212
12	Trnava	Jendrašiček	148	1956–1998 (42)	0.405	6.64	26.6 (1979)	14.1	24.4	34.1
13	Gliboki Potok	Mlačine	84	1970–1998 (29)	0.731	19.2	34.2 (1986)	29.9	36.3	41.8
14	Koprivnica	Koprivnica	122	1951–1998 (46)	0.645	23.5	55.9 (1963)	45.4	72.2	106
15	Komarnica	Novigrad Podravski	48	1958–1998 (40)	0.288	9.39	26.3 (1963)	19.1	35.7	59.1
16	Voćinka	Mikleuš	173	1960–1998 (39)	2.18	54.5	107 (1972)	93	113	124
17	Vojlovica	Čačinci	150	1968–1998 (28)	1.9	35.9	90 (1975)	61	90.1	115
SAVA RIVER BASIN										
18	Sava	Jesenice	10750	1964–1995 (32)	276	1846	3489 (1964)	2680	3745	4692
19	Sava	Podsused	12316	1949–1995 (47)	306	1738	3332 (1990)	2571	3485	4747
20	Sava	Zagreb	12450	1926–1995 (70)	314	1775	3126 (1964)	2348	3073	3633
21	Sava	Rugvica	12712	1926–1995 (67)	312	1502	2357 (1990)	2069	2662	3327
22	Sava	Crnac	22852	1955–1992 (38)	529	1935	2331 (1991)	2145	2360	2481
23	Sava	Jasenovac	38958	1926–1991 (64)	784	1977	2716 (1970)	2291	2678	3052
24	Sava	Stara Gradiška	40100	1937–1991 (54)	788	1899	2524 (1974)	2214	2588	2921
25	Sava	Mačkovac	40838	1951–1990 (40)	823	2115	3018 (1974)	2519	3026	3438
26	Sava	Davor	47200	1958–1993 (36)	931	2321	3130 (1974)	2697	3180	3560
27	Sava	Slavonski Kobaš	49031	1926–1993 (65)	974	2411	3260 (1932)	2974	3379	3804
28	Sava	Slavonski Brod	50858	1945–1993 (49)	944	2466	3476 (1974)	2891	3395	3751
29	Sava	Županja	62891	1929–1998 (65)	1159	2942	4161 (1970)	3763	4393	5188
30	Bregana	Bregana Remont	88.5	1970–1998 (29)	1.38	21.5	34.1 (1972)	31.1	41.2	51.8
31	Lipovačka Gradna	Hamor	19.11	1948–1998 (50)	0.381	4.26	7.4 (1989)	6.1	8.75	11.3
32	Rudarska Gradna	Rudarska Draga	15.6	1957–1994 (38)	0.255	4.49	8.79 (1962)	6.88	9.57	11.9
33	Vrapčak	Gornje Vrapče	11.7	1970–1998 (29)	0.12	3.68	15.4 (1975)	6.79	16.1	34.9
34	Vrapčak	Zagreb	15	1961–1998 (38)	0.168	4.73	17.4 (1975)	7.15	13.4	18.4
35	Črnomerec	Frateršćica	7.37	1953–1998 (46)	0.084	2.18	8.42 (1954)	4.21	11.6	27.3
36	Kustošak	Kustošija	6.08	1956–1998 (32)	0.054	2.58	10 (1961)	6.49	12.7	25.3
37	Medveščak	Mihaljevac	14.15	1971–1998 (28)	0.135	3	11.6 (1989)	4.52	11	18.1
38	Bliznec	Markuševac	4.97	1969–1998 (30)	0.076	1.51	5.08 (1995)	3.75	8.52	19
39	Štefanovec	Dubrava	8.03	1961–1994 (30)	0.131	3.61	7.61 (1989)	5.85	8.41	11.2
40	Trnava	Granešina	28.95	1954–1998 (44)	0.31	7.13	27.1 (1980)	12.6	28.2	52
41	Sunja	Sunja	225	1965–1998 (31)	2.84	87.5	141 (1972)	134	177	208
42	Šumetlica	Cernik	33.5	1972–1998 (27)	0.291	6.45	13.7 (1986)	9.8	15	19.9
43	Sutla	Brezno	109	1946–1975 (30)	1.34	21.8	38.6 (1969)	31.4	40.3	49.8
44	Sutla	Miljana	263	1947–1976 (30)	4.19	65.8	77 (1964)	70.9	76.1	80
45	Sutla	Zelenjak	455	1958–1998 (41)	7.27	123	250 (1964)	184	246	310
46	Krapina	Kupljenovo	1150	1964–1998 (35)	11.8	154	268 (1989)	207	274	329
47	Zelina	Božjakovina	186	1957–1998 (38)	1.64	28.9	47.9 (1959)	44.8	64.9	86.5
48	Lonja	Bisag	88.8	1952–1982 (31)	0.768	15.6	22.8 (1966)	18.9	21.5	22.9
49	Lonja	Lonjica	326	1972–1998 (27)	1.88	21.8	52.7 (1976)	27.7	51.3	69.6
50	Česma	Narta	881	1958–1998 (41)	5.43	51.1	104 (1993)	70.6	99.7	123
51	Česma	Čazma	2877	1963–1998 (36)	15.1	98.3	171 (1993)	147	197	256
52	Ilova	Veliko Vukovje	995	1945–1998 (52)	7.36	71.5	151 (1972)	89.6	139	169
53	Bijela	Badljčina	170	1969–1998 (30)	1.61	23.6	36.7 (1980)	30.5	33.7	35.1
54	Orljava	Pleternica	745	1970–1998 (29)	5.25	63.4	117 (1987)	98.2	120	139
55	Londža	Pleternica	483	1973–1998 (25)	1.87	36.8	87.2 (1987)	64.3	101	138
56	Una	Hrvatska Kostajnica	8876	1926–1991 (65)	228	1138	1808 (1955)	1392	1677	1823

No.	River	Gauging station	Catchment area (km ²)	Observing period (no. of years)	Discharges Q (m ³ s ⁻¹)			Maximum for return periods (years)		
					Mean	Average max annual	Max obs'd (year of occurrence)	10	100	1000
KUPA RIVER BASIN										
57	Kupa	Kupari	208	1951–1998 (48)	13.5	141	195 (1966)	170	199	222
58	Kupa	Hrvatsko	370	1957–1998 (40)	20.5	287	419 (1966)	384	485	599
59	Kupa	Petrina	528	1951–1992 (42)	26.6	455	1079 (1952)	641	898	1140
60	Kupa	Radenci	1304	1951–1992 (42)	53.7	647	920 (1968)	809	945	1034
61	Kupa	Pribanji	1492	1949–1985 (37)	61.8	675	1021 (1966)	862	1028	1167
62	Kupa	Ladešić Draga	1590	1956–1998 (42)	58.4	700	1010 (1966)	851	975	1049
63	Kupa	Kamanje	2192	1957–1998 (40)	73.3	811	1145 (1966)	967	1139	1266
64	Kupa	Brodarci	3405	1957–1998 (41)	110	944	1237 (1968)	1160	1305	1419
65	Kupa	Rečica	5923	1948–1982 (35)	171	1137	1533 (1966)	1450	1667	1791
66	Kupa	Jamnička Kiselica	6805	1948–1978 (31)	180	967	1581 (1953)	1416	1791	2351
67	Kupa	Šišinec	7274	1950–1991 (41)	182	949	1259 (1974)	1114	1338	1503
68	Kupa	Farkašić	8902	1965–1992 (26)	196	1048	1631 (1974)	1281	1593	1839
69	Kupa	Brest	9021	1926–1974 (49)	206	1006	1523 (1974)	1204	1382	1481
70	Čabranka	Zamost	103	1950–1998 (49)	3.72	76	128 (1984)	115	143	169
71	Kupica	Brod na Kupi	291	1951–1998 (48)	13.7	146	357 (1993)	194	293	377
72	Kupčina	Strmac	125	1959–1998 (40)	2.18	22.7	45.8 (1974)	38.7	57.4	88
73	Kupčina	Lazina Brana	169	1973–1998 (26)	2.07	22.9	28.8 (1989)	27.7	30.8	32.4
74	Križ Potok	CP Križ	5.4	1963–1998 (36)	0.312	14.3	28.3 (1982)	22.5	29.9	37.6
75	Vela Voda	Crni Lug	3.7	1963–1998 (36)	0.208	7.98	12.7 (1965)	12	16.8	22.4
76	Bela Voda	Crni Lug	1.8	1963–1998 (36)	0.106	5.42	9.78 (1963)	9.13	11.5	14.3
77	Leska	Leska	0.25	1963–1998 (26)	0.015	0.603	1.31 (1963)	0.933	1.44	1.92
78	Klada	Klada	0.33	1963–1998 (26)	0.018	0.443	1.2 (1963)	0.904	1.49	2.34
79	Gornja Dobra	Luke	175	1947–1998 (51)	7.04	109	166 (1968)	135	161	179
80	Gornja Dobra	Turkovići	296	1963–1998 (33)	10	118	154 (1998)	148	178	205
81	Vitunjčica	Brestovac	34	1967–1998 (31)	3.28	31.3	40 (1998)	36.8	39.6	41.9
82	Donja Dobra	Trošmarija	821	1960–1998 (39)	27.9	163	246 (1966)	194	226	246
83	Donja Dobra	Donje Stative	1049	1960–1998 (39)	34.9	249	372 (1966)	309	393	451
84	Ribnjak	Lučanjek	50	1948–1975 (27)	3.01	16.4	25.7 (1962)	22.8	28.5	33.8
85	Globornica	Generalski Stol	32	1949–1975 (27)	1.02	18.8	31.4 (1966)	30.7	42.5	60.6
86	Mrežnica	Juzbašići	683	1947–1998 (46)	12.4	92.4	166 (1989)	122	148	166
87	Mrežnica	Mrzlo Polje	975	1947–1998 (52)	29.5	254	373 (1974)	329	390	445
88	Tounjčica	Ožanići	118	1948–1975 (28)	10.4	70.1	95.6 (1952)	89.4	98.8	108
89	Munjavčica	Josipdol	44.1	1948–1975 (27)	0.431	3	5.84 (1968)	4.85	6.78	9.06
90	Korana	Korana	232	1952–1986 (35)	3.09	19.2	36.2 (1957)	28	37.4	50.5
91	Korana	Slunj	614	1964–1998 (29)	11.1	137	271 (1973)	217	298	402
92	Korana	Veljun	943	1949–1998 (44)	23	264	460 (1955)	363	438	495
93	Korana	Velemerić	1297	1946–1997 (46)	28.8	327	571 (1948)	453	616	769
94	Plitvice – Kozjak	Kozjak Most	169	1953–1991 (33)	3.55	16.2	28.9 (1955)	24.2	33.2	40
95	Plitvice – Matica	Plitvički Ljeskovac	20.6	1952–1991 (37)	2.42	12	49.5 (1976)	14.3	23.4	29.7
96	Slunjčica	Slunj	220	1949–1983 (35)	9.48	58.5	80 (1962)	72.6	80.6	86.5
97	Radonja	Tušilović	224	1967–1998 (26)	3.32	27.5	40.7 (1987)	35.1	43.6	50.2
98	Glina	Maljevac	183	1953–1986 (34)	3.37	38.5	90.6 (1959)	52.7	82.4	108
99	Glina	Vranovina	889	1947–1998 (45)	14.1	146	344 (1974)	275	411	619
100	Glina	Glina	1145	1952–1998 (40)	18.3	178	395 (1955)	290	438	607

RESULTS

By applying the described methodology, Creager's and Francou-Rodier's envelope curves of maximum specific discharges and maximum discharges were defined for average maximum annual discharges, for the highest observed discharges and for maximum annual discharges of the 10, 100 and 1000-year return periods. The results obtained are shown in Figs 2, 3, 4 and 5.

The summary overview of the calculated regional parameters a , b , c of Creager's formula, and K of Francou-Rodier's formula is shown in Table 2.

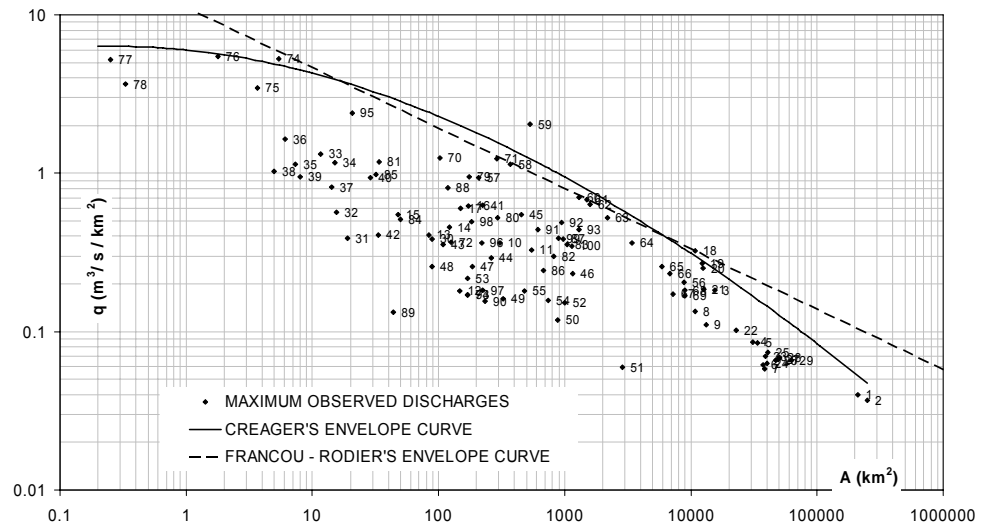


Fig. 2 Creager's and Francou-Rodier's envelope curves of maximum observed specific discharges in the Danube River basin in Croatia.

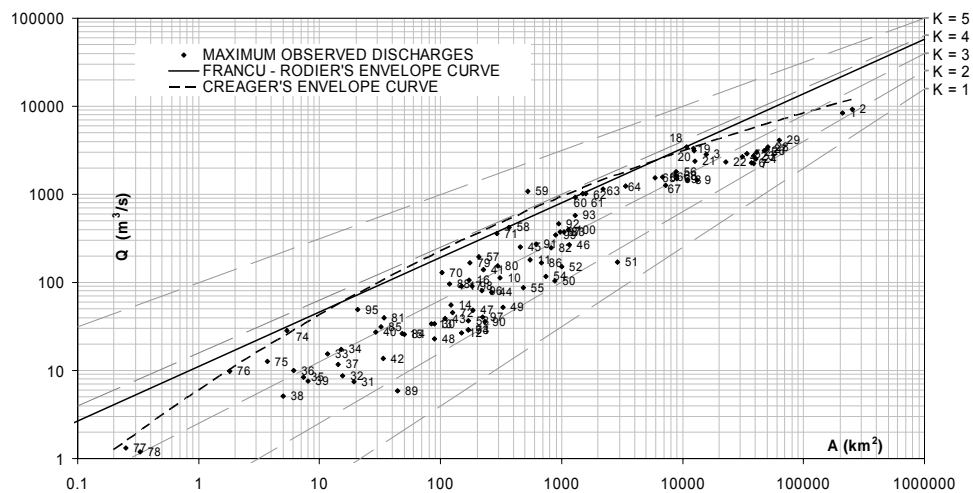


Fig. 3 Creager's and Francou-Rodier's envelope curves of maximum observed discharges in the Danube catchment area in Croatia

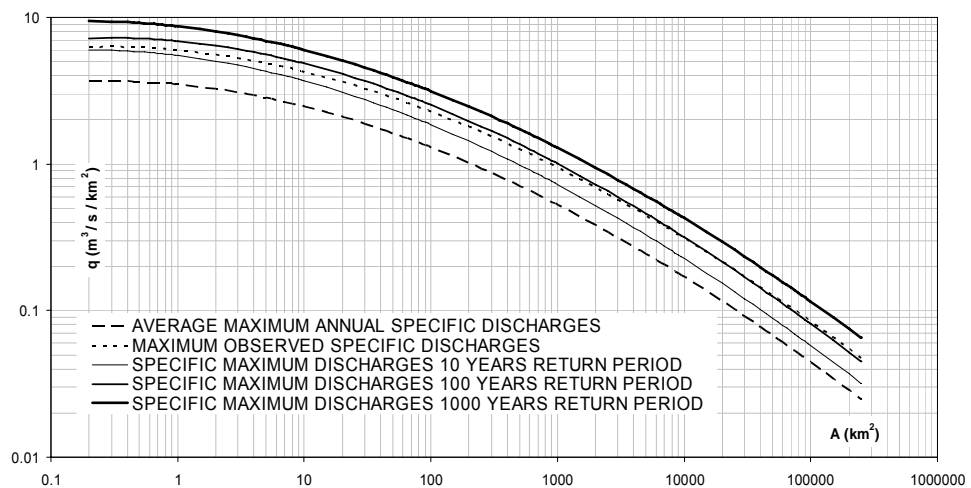


Fig. 4 Creager's envelope curves of maximum specific discharges in the Danube River basin in Croatia.

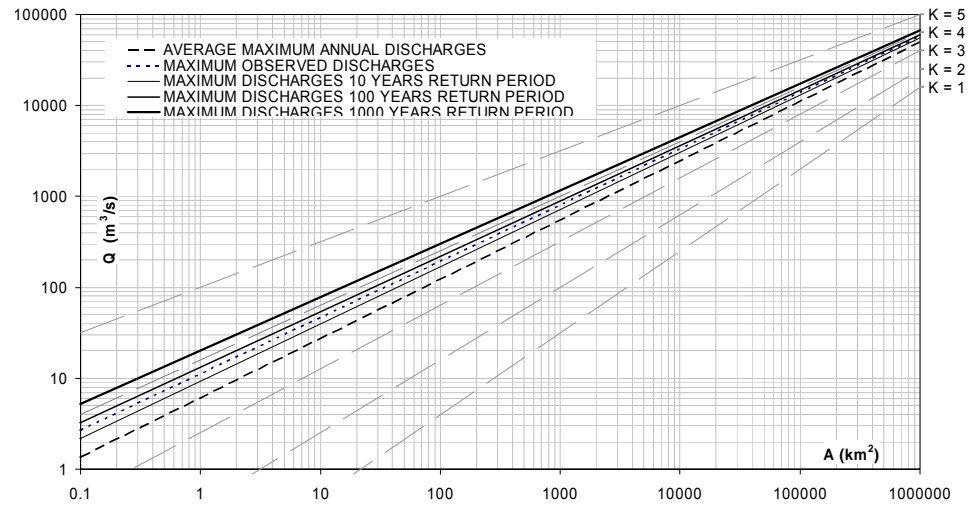


Fig. 5 Francou-Rodier's envelope curves of maximum discharges in the Danube River basin in Croatia.

Table 2 Summary overview of calculated regional parameters.

Discharges	Creager's formula			Francou-Rodier formula K
	a	b	c	
Average maximum annual	3.5	0.918	-0.034	3.478
Maximum observed	6.0	0.920	-0.033	3.808
Maximum of 10-year return period	5.5	0.894	-0.034	3.711
Maximum of 100-year return period	6.9	0.919	-0.035	3.899
Maximum of 1000-year return period	8.7	0.903	-0.032	4.132

CONCLUSION

The relationships presented in this paper were calculated on the basis of 99 available and sufficiently long homogenous time series of observed discharges at gauging stations on the Danube River basin in Croatia and can be used for evaluation of the reliability of previously calculated maximum discharges for this area. Comparisons between the calculated envelope curves show that the Francou-Rodier envelopes give smaller values of maximum discharges than Creager's envelopes for all catchment areas except very small and very large ones.

Because of the climate, relief and geological diversity of the investigated area, further studies of envelope curves of maximum discharges in the Danube River basin in Croatia should be directed to sub-regionalization. Further regional studies of flood characteristics in the Danube catchment area in Croatia should be also directed to analysis of flood wave volumes and durations.

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