

# Guidelines for the use of units, symbols and equations in hydrology\*

## 1. Physical dimensions and units

- (a) Make sure that all quantities are dimensionally correct and that relationships thereof, expressed in equations, are dimensionally consistent. In particular, distinguish between stocks and fluxes. For example precipitation ( $P$ ), evaporation ( $E$ ) and runoff ( $Q$ ) rates are fluxes [ $L^3T^{-1}$  or  $LT^{-1}$ ], whereas storage ( $S$ ) is a stock [ $L^3$  or  $L$ ] and storage variation in time  $t$ ,  $dS/dt$ , is a flux (so that  $dS/dt = P - E - Q$  is correct, whereas  $\Delta S = P - E - Q$  is not).
- (b) Use SI units or SI derived units.
- (c) Use s, min, h, and d (rather than sec, mins, hr/hrs, day/days) for second, minute, hour and day respectively. Do not abbreviate week, month or year, which are non SI units.<sup>†</sup>
- (d) Multiplication of units should be indicated by a space, e.g. N m, and division either by negative exponents (e.g.  $m\ s^{-2}$ ) or by use of the solidus (oblique line, e.g.  $m/s^2$ ); however repeated use of the solidus (e.g.  $m/s/s$ ) is not permitted. The convention adopted must be used consistently throughout.
- (e) Prefixes of units such as M (mega =  $10^6$ ) and  $\mu$  (micro =  $10^{-6}$ ) have no space between (e.g.  $\mu s$ , MW). Note that, according to SI, any power to a unit applies also to the prefix. Note also that the prefix kilo is lower case k (e.g. km, not Km—the upper case K is the symbol of the kelvin).
- (f) For areas and volumes use  $m^2$  and  $m^3$ , if necessary multiplied by a power of 10, using multiples of 3 for the power of 10. Alternatively use prefixed units where appropriate, e.g.  $km^2$  for square kilometres,  $km^3$  (cubic kilometres) for billion cubic metres, etc.; note that a million cubic metres can be written as  $1 \times 10^6\ m^3$  or  $1\ hm^3$  (cubic hectometre) but not  $1\ Mm^3$  (in fact  $1\ Mm^3 = 10^{18}\ m^3$ ). In addition, the hectare (ha)<sup>†</sup> and the litre (L or l) are also allowed in SI.
- (g) All units should be typeset using upright (Roman) fonts, not italic or bold.
- (h) Numerals should also be typeset using upright fonts. The symbol for the decimal marker is the dot. To facilitate reading, numbers may be divided in groups of three using a thin space (e.g. 12 345.6). Neither dots nor commas are permitted as group separators. A space is used to separate the unit from the number (e.g. 10 m, not 10m).

## 2. Symbols and equations

- (a) Prefer single-letter variables (if necessary with subscripts, e.g.  $E_{RMS}$ ) over multi-letter ones (e.g. RMSE). Single-letter variables or parameters and user-defined function symbols should be italic (e.g.  $x$ ,  $Y$ ,  $\beta$ ,  $f(x)$ ). Multi-letter variables, if cannot be avoided, should not be italic.
- (b) Common, explicitly defined, functions should not be italic, whether their symbols are single-letter (e.g.  $\Gamma(x)$  for the gamma function,  $B(y, z)$  for the beta function) or multi-letter (e.g.  $\ln x$ ,  $\exp(x + y)$ ).
- (c) Textual subscripts or superscripts should not be italic (e.g.  $x_{max}$ ,  $T_{min}$  where ‘max’ and ‘min’ stand for maximum and minimum, respectively).
- (d) Mathematical constants should not be italic (e.g.  $e = 2.718\dots$ ,  $\pi = 3.141\dots$ ,  $i^2 = -1$ ). Also, mathematical operators should not be italic (e.g.  $dx$  in integrals and derivatives,  $\Delta\gamma$  for the difference operator on  $\gamma$ ).
- (e) Vectors, matrices and vector functions should be bold and italic (for single-letter variables). In particular, vectors are usually denoted with lower case letters (e.g.  $\mathbf{x}$ ,  $\boldsymbol{\omega}$  as vectors;  $\mathbf{f}(\mathbf{x})$  as a vector function of a vector variable) and matrices with upper case letters (e.g.  $\mathbf{A}$  as matrix;  $\mathbf{AB}$  as the product of matrices  $\mathbf{A}$  and  $\mathbf{B}$ ,  $\mathbf{A}^T$  as the transpose of  $\mathbf{A}$ ,  $\det \mathbf{A}$  as the determinant of a square matrix  $\mathbf{A}$ ).
- (f) To distinguish between random variables and their realizations, either use upper case symbols for the former and lower case for the latter (e.g.  $P\{X \leq x\}$ ), or underline the random variables (e.g.  $P\{\underline{x} \leq x\}$ , the so-called Dutch convention).
- (g) Do not use the hyphen (-) as a minus or subtraction sign; use the en-dash (–) instead. Also do not use the letter ‘x’ or the symbol ‘\*’ as a multiplication sign; either use the symbol ‘ $\times$ ’ or middle dot ( $\cdot$ ) between numerals, or use a thin space (or even no space) between variables.
- (h) For simple expressions in the body of the text, use solidus (/) to denote division, e.g.  $(x + y)/2\eta$ , rather than a fraction with a horizontal division line.
- (i) Write complex exponential functions in the form:  $\exp(\dots)$ , e.g.  $\exp((a + by^2)^{1/2})$  rather than as a power of e. Note that nested parentheses are permitted (even recommended) for grouping.

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<sup>†</sup> Some journals accept ‘a’ as a symbol for year, but ‘a’ is also the symbol of an ‘are’ which is a unit for area not recommended per se but commonly used in its multiple hectare ( $1\ a = 100\ m^2$ ;  $1\ ha = 100\ a = 10^4\ m^2 = 1\ hm^2$ ).